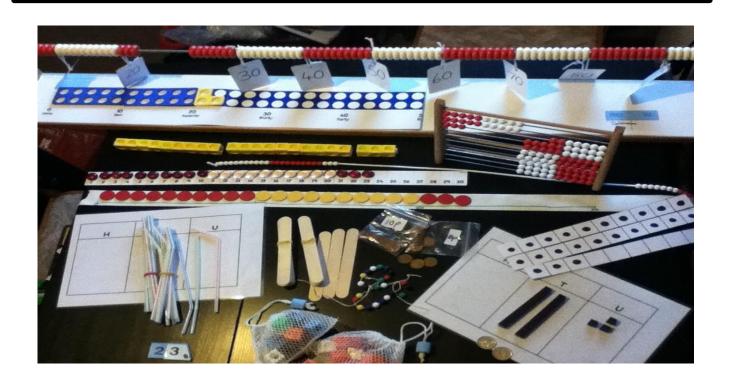
St Augustine's Progression in Calculations Policy Year 1 to Year 6



Aims



The national curriculum for mathematics aims to ensure that all pupils:

- become **fluent** in the fundamentals of mathematics, including through varied and frequent practice with increasingly complex problems over time, so that pupils develop conceptual understanding and the ability to recall and apply knowledge rapidly and accurately.
- reason mathematically by following a line of enquiry, conjecturing relationships and generalisations, and developing an argument, justification or proof using mathematical language
- can solve problems by applying their mathematics to a variety of routine and non-routine problems with increasing sophistication, including breaking down problems into a series of simpler steps and persevering in seeking solutions.

Introduction

Written methods of calculations are based on mental strategies. Each of the operations builds on mental skills which provide the foundation for jottings and informal written methods of recording. Skills need to be taught, practised and reviewed constantly. These skills lead on to more formal written methods of calculation.

Strategies for calculation need to be represented by models and images to support, develop and secure understanding. This, in turn, builds fluency. When teaching a new strategy it is important to start with numbers that the child can easily manipulate so that they can understand the methodology.

The transition between stages should not be hurried as not all children will be ready to move on to the next stage at the same time, therefore the progression in this document is outlined in stages. Previous stages may need to be revisited to consolidate understanding when introducing a new strategy.

A sound understanding of the number system is essential for children to carry out calculations efficiently and accurately.

Magnitude of Calculations

Year 1 – O + O, O + TO (numbers up to 20), 0 - 0, TO – O (numbers up to 20), O x O, $0 \div 0$

Year 2 - TO + O, TO + multiples of 10, TO + TO, O + O + O, TO - O, TO - tens, TO - TO, TO x O, O ÷ O

Year 3 – add numbers with up to three-digits, HTO + multiples of 10, HTO + multiples of 100, subtract numbers up to three-digits, HTO – O, HTO – multiples of 10, HTO – multiples of 100, HTO – HTO, TO \times O, TO \div O

Year 4 - add and subtract numbers with up to four-digits, ThHTO + ThHTO, ThHTO - ThHTO, add and subtract decimals with up to two decimal places in the context of money, multiply three numbers together, TO x O, HTO x O, TO x O, multiply by zero and one, TO \div O, HTU \div O

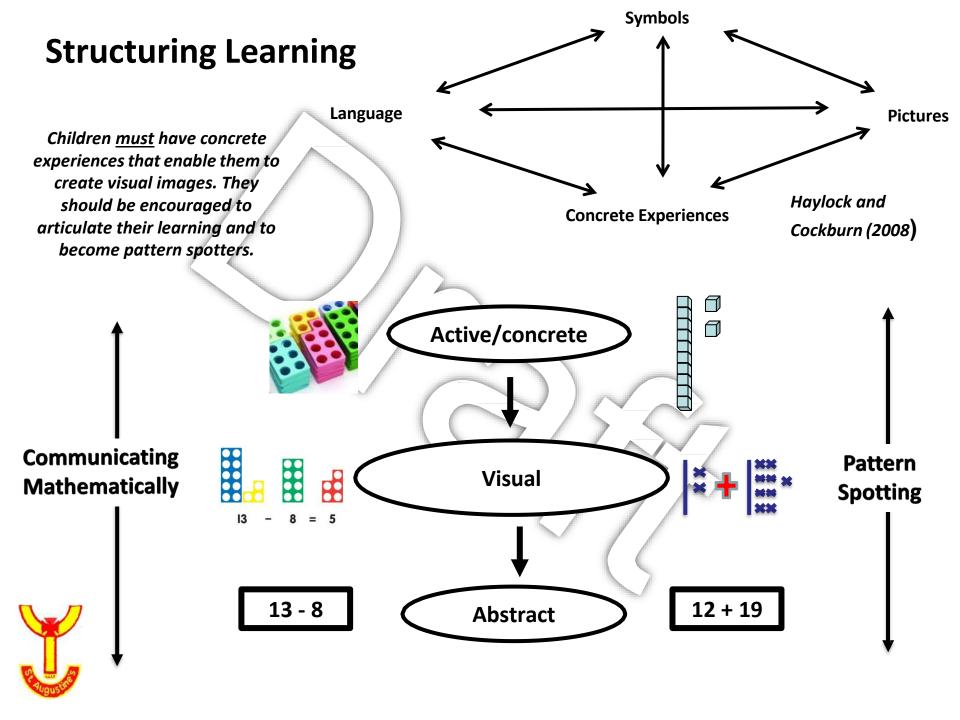
Year 5 – add and subtract numbers with more than four-digits, add and subtract decimals with up to three decimal places, ThHTO x UO ThHTO x TO, HTO x TO, multiply whole numbers and decimals with up to three-decimal places by 10, 100 and 1000, divide numbers with up to four-digits by O (including remainders as fractions and decimals and rounding according to the context)

Year 6 - add and subtract numbers with more than four-digits, add and subtract decimals with up to three decimal places, multiply numbers with up to four-digits by TO, multiply numbers with up to two-decimal places by a whole number, divide numbers up to four-digits by TO (interpreting remainder according to the context), divide decimals up to two-decimal places by O or TO

Mathematics is an interconnected subject in which pupils need to be able to move fluently between representations of mathematical ideas. ... pupils should make rich connections across mathematical ideas to develop fluency, mathematical reasoning and competence in solving increasingly sophisticated problems. They should also apply their mathematical knowledge to science and other subjects.

National Curriculum 2014

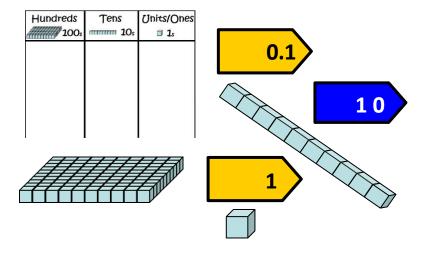




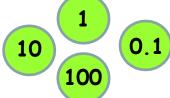
bead string

Multilink

place value apparatus



place value counters





count stick

Cuisenaire

Numicon



double sided counters

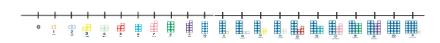
1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	12	53	54	55	56	57	58	59	60
61	12	63	64	65	66	67	68	69	70
71	3E	100	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100
101	102	103	104	105	106	107	108	109	110
111	112	113	114	115	116	117	118	119	120
121	122	123	124	125	126	127	128	129	130
131	132	133	134	135	136	137	138	139	140
141	142	143	144	145	146	147	148	149	150
151	152	153	154	155	156	157	158	159	160
161	162	163	164	165	166	167	168	169	170
171	172	173	174	175	176	177	178	179	180
181	182	183	184	185	186	187	188	189	190
191	192	193	194	195	196	197	198	199	200

11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	13	53	54	55	56	57	58	59	60
61	12	63	64	65	66	67	68	69	70
71	3	100	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

1 2 3 4 5 6 7 8 9 10

number grids 100 and 200

number line

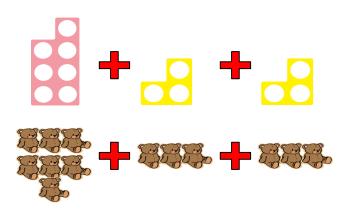


Structures of Addition (Haylock and Cockburn 2008)

Children should experience problems with all the different addition structures in a range of practical and relevant contexts e.g. money and measurement

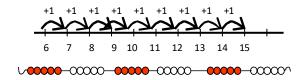
Aggregation

Union of two sets
How many/much altogether?
The total



Augmentation

Start at and count on Increase by Go up by



Commutative law

Understand addition can be done in any order
Start with bigger number when counting on
(Explain to children that subtraction does not have this property)



is the same as/equal to (=)



Addition

Pupils develop the concept of addition and subtraction and are enabled to use these operations flexibly.

Addition and subtraction should be taught together.

End of Year Expectations

Possible Concrete and Visual Representations

'two more

than three is

five or two

less than five

is three'

Use practical resources such as bears, counters,

cubes and number lines/hundred grids and

progress to a resource such as Numicon to

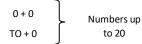
encourage counting in groups rather than ones

2 3 4 5 6 7 8 9 10

Teacher Modelling/Children's Recording

Fluency

Year 1



(including adding zero)
Children must experience combining
two, and then more than two, groups
of objects using counting on and the
language of addition e.g. add, plus
Children must experience
increasing numbers e.g. what is
two more than seven?

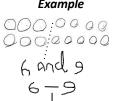
Children should solve one step problems and missing number problems.

Compare quantities to say how many less and/or how many more

If using Numicon, children could use printed
Numicon icons and stick these in - progressing
to recording number sentences alongside



pictorially progressing to recording number sentences alongside



6 7 8 9 10 11 12 13 14 15

Count forwards, to and across 100, beginning with 0 or 1 or from any given number

Switch count between tens and ones e.g. 10, 20, 30, 31, 32, 33 ...

Represent and use number bonds up to 20 (establish addition and subtraction as related operations)

Find one more than a number

Find ten more than a number

Count in multiples of 2s, 5s and 10s starting on multiples to highlight pattern recognition

> Vocabulary: count on, add, and, plus, more, sum, total, altogether,

Year 2

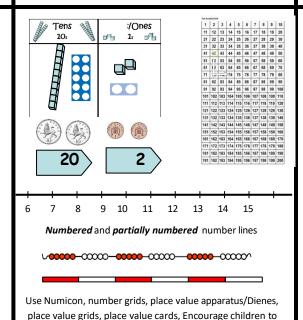
Children should be able to partition numbers in different ways e.g. as 2+2+2+1 or 5+3 or 23 as 20+3 or 10+13

TO + O
TO + tens
TO + TO
O + O + O

Children should use concrete objects, pictorial representations and add numbers in different contexts e.g. money, measures ENSURE CHILDREN HAVE THE OPPORTUNITY TO ADD **MORE** THAN TWO NUMBERS

Children should recognise and use the inverse relationship to solve missing number problems.

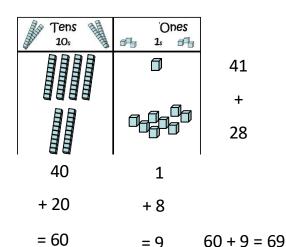
Children should understand the language of sum Ensure children understand that addition is commutative (can be done in any order)



partition numbers rather than counting in ones.

Children apply, develop and secure their understanding of place value

Use jottings and record number sentences



Show increasing fluency in deriving pairs of numbers up to 10 and then up to 20

Use knowledge to derive and use number facts up to 100

Add numbers mentally including TO + O, TO + tens, TO + TO, O + O + O

Vocabulary: count on, add, and, addition, plus, more, sum, total, altogether,



End of Year Expectations

Year 3

Add numbers with up to three-digits (leading to formal written column method)

HTO + multiples of 10 HTO + multiples of 100

ENSURE CHILDREN HAVE THE OPPORTUNITY TO ADD MORE THAN TWO NUMBERS WITH DIFFERING NUMBERS OF DIGITS

Children should partition numbers, up to 1000, in different ways

e.g. 100 + 40 + 6 or 100 + 30 + 16

Solve problems in different contexts including missing number problems

Year 4

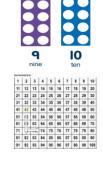
Add numbers with up to fourdigits (formal written column method) including numbers with up to two decimal places in the context of money

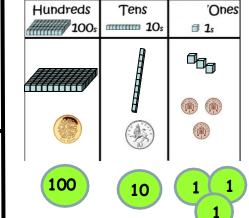
ENSURE CHILDREN HAVE THE OPPORTUNITY TO ADD **MORE THAN** TWO NUMBERS INCLUDING DECIMALS, WITH DIFFERING NUMBERS OF DIGITS

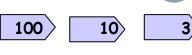
Solve two-step problems in different contexts including missing number problems

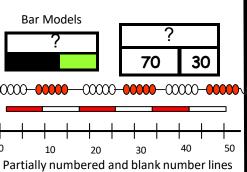
Possible Concrete and Visual Representations











Teacher Modelling/Children's Recording

Children apply, develop and secure their understanding of place value and begin to record in columns

Manipulatives SHOULD be used alongside algortihms

Column addition (no exchanging) with up to three-digits

Expanded recording without exchange

Expanded recording with exchange

$$\begin{array}{c}
100 + 40 + 1 \\
100 + 20 + 8 \\
\hline
200 + 60 + 9 = 269
\end{array}$$

Add decimals in the

context of money

Expanded recording

Compact (column) recording

Column addition (with exchanging)

Compact (column) recording

Count in ones, tens and hundreds maintaining fluency through varied and frequent practice

Fluency

Count from 0 in multiples of 4, 8, 50 and 100

Find 10 or 100 more than a number

Mentally add HTO + ones, HTO + tens, HTO + hundreds

Perform mental calculations with twodigit numbers, the answer could exceed 100

Vocabulary: count on, add, and, addition, addend addend, plus, more, sum, total, altogether,

Count in 6s, 7s, 9s, 25s and 100s

Find 1000 more than a number

Perform mental calculations with increasingly large numbers to aid fluency

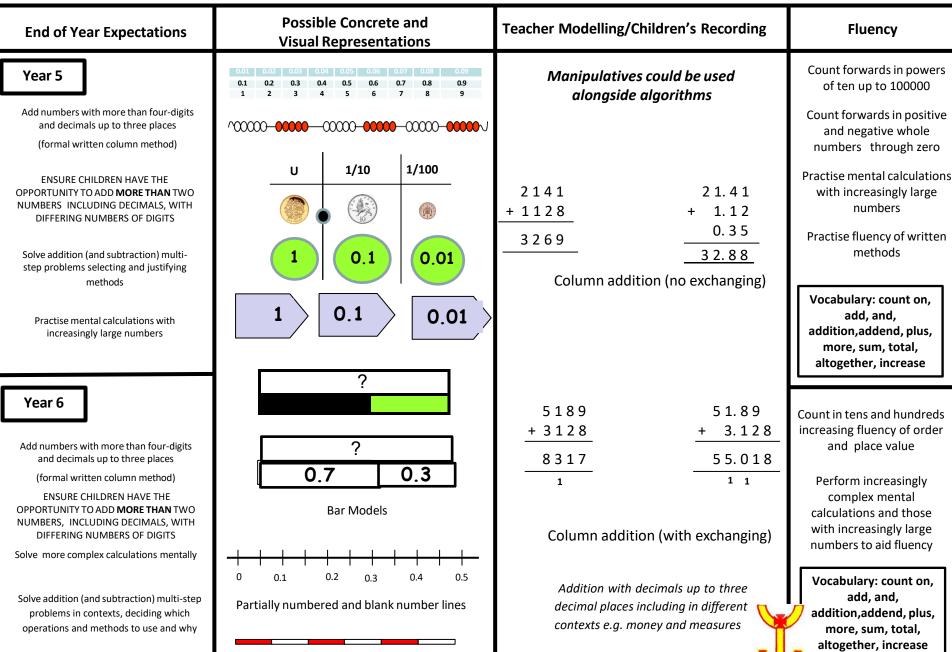
Vocabulary: count on, add, and, addition, addend, plus, more, sum, total, altogether,

10

Addition

Pupils develop the concept of addition and subtraction and are enabled to use these operations flexibly.

Addition and subtraction should be taught together.



Structures of Subtraction (Haylock and Cockburn 2008)

Children should experience problems with all the different subtraction structures in a range of practical and relevant contexts e.g. money and measurement

Partitioning

Take away
... how many left?
How many are not?
How many do not?







Comparison

What is the difference?
How many more?
How many less (fewer)?
How much greater?
How much smaller?



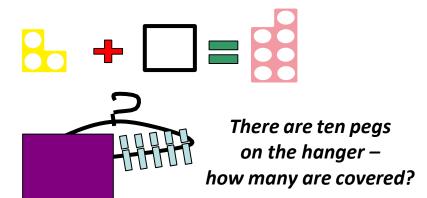




'two more than three is five or two less than five is three'

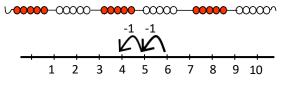
Inverse-of-addition

What must be added?
How many (much) more needed?



Reduction

Start at and reduce by
Count back by
Go down by



Pupils develop the concept of addition and subtraction and are enabled to use these operations flexibly. **Subtraction** Addition and subtraction should be taught together. Possible Concrete and **End of Year Expectations** Teacher Modelling/Children's Recording **Fluency Visual Representations** Count backwards (including Children may begin recording O- O Year 1 crossing 100) any given number pictorially progressing to recording TO - O Switch count between ones and number sentences alongside tens e.g. 33, 32, 31, 30, 20, 10 0 10 Numbers up to 20 Represent and use subtraction (including subtracting zero) facts linked to number bonds up to 20 (establish addition and subtraction as related V-00000-00000-00000-00000-00000^ operations) Understand subtraction as 'two more Find one less than a number taking away 1 2 3 4 5 6 7 8 9 10 than three is What is ... less than ...?) five or two Find ten less than a number 7 less than five Count back in multiples of 2s, 5s is three' and 10s starting on multiples to Compare quantities to say highlight pattern Children could use printed how many less and/or how Numicon icons and stick these in, many more Vocabulary:, leave, take Use practical resources such as bears, counters, again progressing to recording away, fewer, subtract, cubes and number lines/hundred grids and progress number sentences alongside minus, count back, difference to a resource such as Numicon to encourage counting between back in groups rather than ones Children apply, develop and secure their Year 2 TO - O understanding of place value and begin to TO - tens Finding the difference record using jottings and number sentences Practise addition and Tens TO - TO subtraction facts to 20 10s 16 - 3 Understand subtraction Show increasing fluency in as taking away deriving subtraction facts and finding the difference for numbers up to 10 and no exchanging then up to 20 Ensure children understand that Use known facts to 20 to subtraction is not commutative (can derive new facts e.g. 3 + 7 not be done in any order) 30 + 70Use knowledge to derive Children should be able to partition 20 and use subtraction number numbers in different ways

10

11 12 13

Numbered and partially numbered number lines

V-00000-00000-00000-00000-00000^

Children should use concrete materials and pictorial

representations, and use numbers in different contexts e,g, money and measures, Encourage children to partition numbers rather than counting in ones.

15

facts up to 100

26 - 8

exchanging

9

exchange

ten ones

ten for

Vocabulary: subtraction, leave, take away, fewer, subtract, minus, count back, difference between

Subtraction

Pupils develop the concept of addition and subtraction and are enabled to use these operations flexibly.

Addition and subtraction should be taught together.

End of Year Expectations

Possible Concrete and Visual Representations

Tens

10s

10

^00000-00000-00000-00000-00000-00000\J

30

20

10

Ones

1 2 3 4 5 6 7 8 9 10

74 75 76 77 78 79 80

1 1s

واو

100

30

40

50

1 2 3 4 5 6 7 8 9 10

11 12 13 14 15 16 17 18 19 20

31 32 33 34 35 36 37 38 39 40

41 42 43 44 45 46 47 48 49 50

121 122 123 124 125 126 127 128 129 130 131 132 133 134 135 136 137 138 139 140

141 142 143 144 145 146 147 148 149 150

151 152 153 154 155 156 157 158 159 160

161 162 163 164 165 166 167 168 169 170

171 172 173 174 175 176 177 178 179 180

181 182 183 184 185 186 187 188 189 190

191 192 193 194 195 196 197 198 199 200

Hundreds

100s

411111111

100

Bar Models

10

Teacher Modelling/ Children's Recording

Fluency

Count back in ones, tens

and hundreds maintaining fluency through varied and

frequent practice

Switch count between

hundreds, tens and ones

e.g 500, 400, 300, 290, 280,

270, 269, 268, 267

Mentally add HTU + ones,

HTU + tens,

HTU + hundreds

Perform mental calculations

with two-digit numbers, the

answer could exceed 100

Find ten and a hundred less

than a number with up to

three-digits

Vocabulary:

subtraction, leave, take

away, fewer, subtract,

minus, count back, difference between,

minuend, subtrahend

Count back in 6, 7, 9,

25 and 1000

Count back through zero

Year 3

Subtract numbers with up to three-digits

(formal written column method)

HTO - O

HTO – multiples of 10

HTO – multiples of 100

HTO – HTO

Children apply, develop and secure their understanding of place value and begin to record in columns Children SHOULD use manipulatives alongside algorithms

to transition between practical and abstract



8

with exchanging

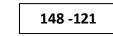
60

$$\frac{20}{30} = \frac{8}{30}$$

$$40$$
 and $5 = 45$

Column subtraction

(no exchanging)



148

Year 4

Subtract numbers with up to four-digits including up to two decimal places in the context of money

(formal written column method)

Understand subtraction as the inverse of addition

Solve two-step problems deciding upon the appropriate operations and methods and justifying choices made Column subtraction (with exchanging)

300 and 50 and 6 = 356

Ensure children can solve calculations where zero is a place holder

to include negative numbers
Find 1000 less than a

number

Continue to practise

mental calculations with

increasingly large

Vocabulary: subtraction, leave, take away, fewer, subtract, minus, count back, difference between, minuend, subtrahend.

numbers to aid fluency

Subtraction

Pupils develop the concept of addition and subtraction and are enabled to use these operations flexibly.

Addition and subtraction should be taught together.

End of Year Expectations

Year 5 Subtract numbers with more than four-digits

Subtract numbers with up to three decimal places

^00000-00000-

U

-00000**-00000**-00000-**00000**V

1/10

0.1

0.7

0.2

0.1

Bar Models

0.3

1/100

0.01

0.01

0.3

0.4

0.5

Subtract larger numbers with more than four digits and those involving numbers up to three decimal places

(formal written column method)

ENSURE CHILDREN HAVE THE
OPPORTUNITY TO ADD MORE THAN
TWO NUMBERS INCLUDING
DECIMALS, WITH DIFFERING
NUMBERS OF DIGITS

Solve (addition) and subtraction multistep problems selecting and justifying methods

Year 6 Subtract numbers with more than four-digits

Subtract numbers with up to three decimal places

Subtract multi-digit numbers including numbers with up to three decimal places

(formal written column method)

ENSURE CHILDREN HAVE THE
OPPORTUNITY TO ADD MORE THAN
TWO NUMBERS INCLUDING DECIMALS,
WITH DIFFERING NUMBERS OF DIGITS

Solve (addition) and subtraction multi-step problems in contexts, deciding which operations and methods to use and why

Teacher Modelling/ Children's Recording

Children might use manipulatives alongside algorithms

Column subtraction (no exchanging)

Column subtraction (with exchanging)

Ensure children can solve calculations where zero is a place holder



Column subtraction (no exchanging)

Column subtraction (with exchanging)

Subtraction with decimals up to three decimal places including in different contexts e.g. money and measures

Count backwards in powers of ten up to one million

Fluency

Count backwards in positive and negative whole numbers through zero

Practise mental calculations with increasingly large numbers

Vocabulary:
subtraction, leave, take
away, fewer, subtract,
minus, count back,
difference
between,minuend,
subtrahend.

Undertake mental calculations with increasingly large numbers and more complex calculations

Vocabulary: subtraction, leave, take away, fewer, subtract, minus, count back, difference between, minuend, subtrahend.

Structures of Multiplication (Haylock and Cockburn 2008)

Children should experience problems with all the different multiplication structures in a range of practical and relevant contexts e.g. money and measurement

Repeated addition

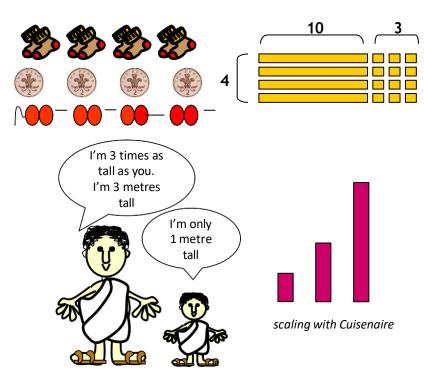
So many lots (sets) of so many How many (how much) altogether Per, each

Scaling

Scaling, scale factor
Doubling, trebling
So many times bigger than (longer than,
heavier than, and so on)
So many times as much as (or as many as)

Commutative law

Scaling, scale factor
Doubling, trebling
So many times bigger than (longer than,
heavier than, and so on)
So many times as much as (or as many as)



a x b and b x a are equal



 4×2 is the same as/equal to 2×4

Multiplication – refer to structures of multiplication

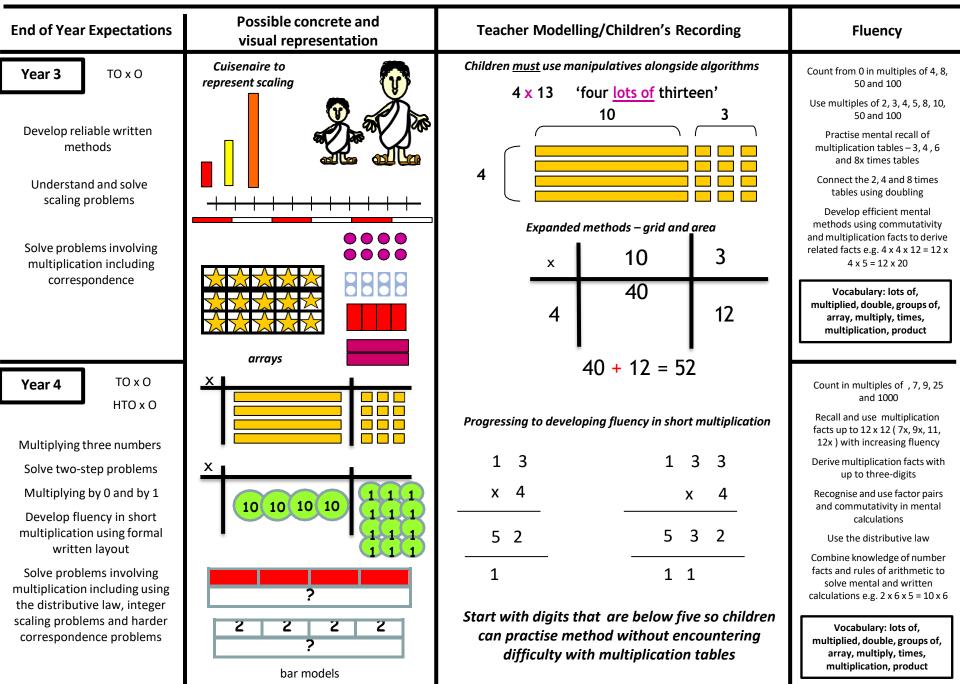
Possible concrete and visual Children's Recording **End of Year Expectations Fluency** representation Practical only e.g. link to small world Year 1 Count in twos, fives and 0×0 tens from different Using concrete objects, pictorial multiples representations and arrays with the support of Numbers up to 20 an adult – take photographs/draw pictures – if e.g. 6, 8, 10, 12 etc using Numicon small icons could be stuck in Solve single step practical problems Emphasise number involving multiplication patterns counting four lots of Double number and in twos Use concrete objects, pictorial two is eight quantities representations arrays- Numicon, Make connections between arrays, Cuisenaire, counters Vocabulary: lots of, number patterns and counting in 6 multiplied, double, twos, fives and tens groups of, array, multiply, times, track with cuisenaire multiplication Double numbers and quantities flexible array Count in twos, fives from zero Year 2 TO x O and tens from any number Record practical work as number sentences e.g. 6, 8, 10, 12 etc Understand multiplication as repeated addition **Emphasise** number patterns $2 + 2 + 2 + 2 = 4 \times 2$ Calculate mathematical statements $4 \times 2 = 8$ two add two add two add two for multiplication within the tables Introduction to multiplication = four lots of two $2 \times 4 = 8$ and write them using symbols tables. Practise to become fluent in multiplication facts Understand and solve 5 10 15 for 2, 5 and 10 problems involving arrays Solve multiplication problems Ensure children understand that mentally multiplication is commutative (can be Vocabulary: lots of, done in any order) multiplied, double, groups Understand that multiplication and of, array, multiply, times,

multiplication

flexible array

division are inverse operations

Multiplication – multiplication and division should be taught together – refer to structures of multiplication



Multiplication - multiplication and division should be taught together-refer to structures of multiplication

End of Year Expectations

Year 5

Th H T O x O

H T O x T O

Th H T O x T O

Multiply decimals with up to three decimal places

Identify multiples and factors including finding all factor pairs of a number, and common factors of two numbers

Solve problems involving all four operations where larger numbers are used by decomposing them into their factors

Multiply whole numbers and those involving decimals by 10, 100 & 1000 $\,$

Understand and use multiplication and division as inverses including in problems involving missing numbers and balancing equations

Solve problems involving multiplication and division including scaling by simple fractions

Know and use the vocabulary of prime numbers, prime factors and composite (non-prime)

Recognise and square and cube numbers and associated notation

Year 6

Multiply numbers up to 4-digit x TO

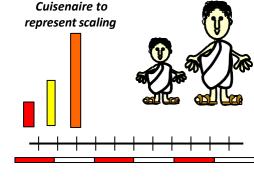
Multiply numbers with up to two decimal places x whole number

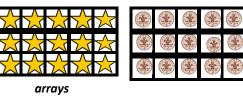
Multiply multi-digit numbers up to fourdigits by a two-digit whole number

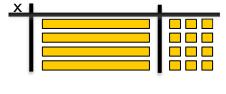
Multiply single –digit numbers with up to two-decimal places by whole numbers

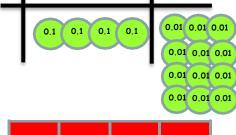
Solve problems involving all four operations

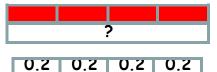
Possible concrete and visual representation











bar models

Teacher Modelling/Children's Recording

${\it Children \ might \ use \ manipulatives \ alongside \ algorithms}$

Short multiplication

1 3 2 4

х 6

7 9 4 4

1 1 2

Short multiplication

3.24

1 0 1 1

1 2

Long multiplication

1 3 2 4

7 9 4 4

2648

3 4 4 2 4

1 1 1

Long multiplication

3.24

x 2 6

1 9 4 4

6 4.8 0

8 4.2 4

1

1

Count forwards in steps of powers of 10 from any given number up to 1 000 000

Fluency

Practise and extend use of formal written method of short multiplication

Apply all multiplication tables frequently. Commit them to memory and use them confidently to make larger calculations

Multiply numbers mentally drawing upon known facts

Vocabulary: lots of, multiplied, double, groups of, array, multiply, times, multiplication, product

Undertake mental calculations with increasingly large numbers

Continue to use all multiplication tables to calculate mathematical statements in order to maintain fluency

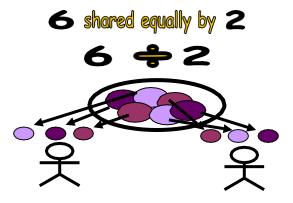
Vocabulary: lots of, multiplied, product, double, groups of, array, multiply, times, multiplication

Structures for Division (Haylock and Cockburn 2008)

Children should experience problems with the different division structures in a range of practical and relevant contexts e.g. money and measurement

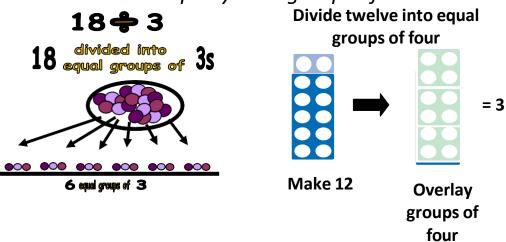
Equal-sharing

Sharing equally between How many (much) each?



Inverse of multiplication (Grouping)

So many lots (sets/groups) of so many Share equally in to groups of ...



Ratio structure

comparison
inverse of scaling structure of multiplication
scale factor (decrease)

Barney earns three times more than Fred. If Barney earns £900 how much does Fred earn?

Jo's journey to school is three times as long as Ella's. If Jo walks to school in 30 minutes how long does it take Ella?

Division

End of Year Expectations

Possible concrete and visual representation

Teacher Modelling/Children's Recording

Fluency

Count in twos, fives and

tens from different

multiples

e.g. 6, 8, 10, 12 etc

Emphasise patterns

Year 1

Solve single step practical problems involving division

Use concrete objects, pictorial representations

> Understand division as grouping and sharing

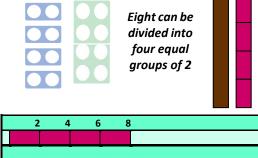
Use the language of 'sharing equally between'

Find halves and then quarters

countina in groups of twos arrays- Numicon, Cuisenaire, counters flexible array

Practical only e.g. link to small world

Using concrete objects, pictorial representations and arrays with the support of an adult – take photographs/draw pictures – if using Numicon small icons could be stuck in



track with cuisenaire

Double numbers and quantities

Find simple fractions of objects, numbers and quantities

Year 2

Solve single step practical problems involving division Use concrete objects, pictorial representations

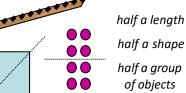
Understand division as grouping

Find halves and then quarters

Work with a range of materials and contexts in which multiplication and division relate to grouping and sharing discrete quantities e.g. marbles, sweets, cherries and continuous quantities e.g. cakes, pizzas, chocolate bars and relate to fractions and measures

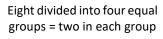
straw bundles





Record as number sentences using ÷ and =

 $8 \div 4$



 $8 \div 4 = 2$

zero and tens from any number

e.g. 12, 10, 8, 6 etc

Count back in twos, fives from

Emphasise patterns

Connect ten times table to place value and five times table to divisions on a clock face

Introduction to multiplication tables. Practise to become fluent in division facts for 2, 5 and 10

Solve division problems involving grouping and sharing

Division - multiplication and division should be taught together- refer to structures of division

Possible concrete and visual **End of Year Expectations** Children's Recording **Fluency** representation Year 1 $0 \div 0$ Count in twos, fives and tens from different Practical only e.g. link to small world multiples Solve single step practical problems involving division Using concrete objects, pictorial e.g. 6, 8, 10, 12 etc representations and arrays with the support of Use concrete objects, pictorial **Emphasise patterns** an adult – take photographs/draw pictures – if representations using Numicon small icons could be stuck in Understand division as Find simple fractions of counting Eight can be objects, numbers and grouping and sharing in groups quantities divided into Use the language of 'sharing of twos four equal equally between' groups of 2 arrays- Numicon, Cuisenaire, counters Find halves and then quarters Vocabulary: equal groups of, divided by, 6 8 lots of, divide, division, halve, half, share equally track with cuisenaire flexible array Count back in twos, threes, fives from Year 2 $0 \div 0$ zero and tens from any number Record as number sentences using ÷ and = e.g. 12, 10, 8, 6 etc Solve single step practical problems **Emphasise patterns** straw bundles involving division $8 \div 4$ Connect ten times table to place value Use concrete objects, pictorial and five times table to divisions on a clock face Eight divided into four equal clock face representations ½ past/ ¼ to ... past groups = two in each group Understand division as grouping Introduction to multiplication tables. five minute divisions Practise to become fluent in division Find halves and then quarters facts for 2, 5 and 10 $8 \div 4 = 2$ Solve division problems involving Work with a range of materials and half a length grouping and sharing contexts in which multiplication and division relate to grouping and sharing half a shape discrete quantities e.g. marbles, sweets, Vocabulary: equal groups of, half a group cherries and continuous quantities e.g. divided by, lots of, divide, of objects division, halve, half, share cakes, pizzas, chocolate bars and relate to

fractions and measures

equally

Fluency

tables)

calculations

quotient.

division with manipulatives

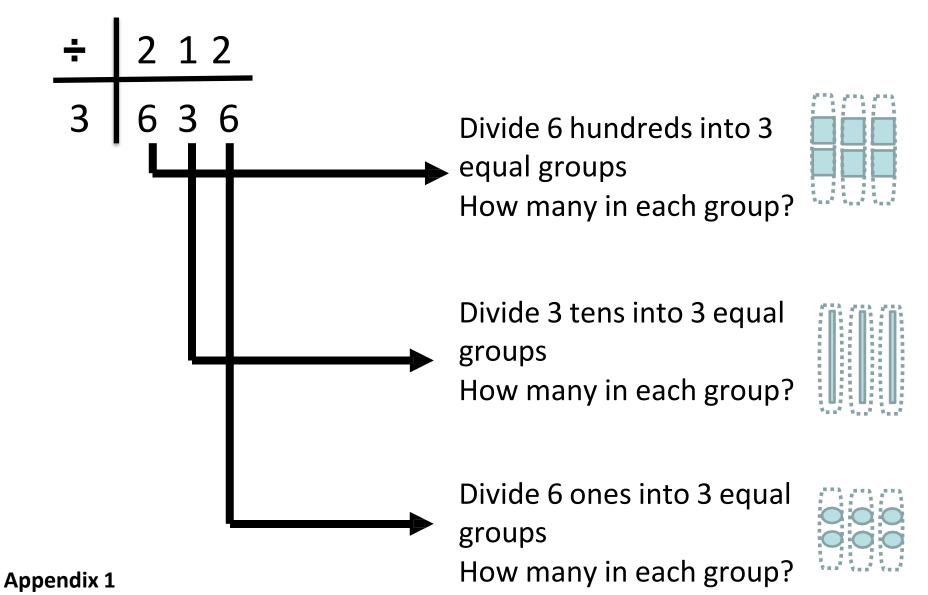
Possible concrete and visual **End of Year Expectations** Teacher Modelling/Children's Recording representation Cuisenaire to Children should use manipulatives Year 3 Recall and use related division $TO \div O$ represent scaling alongside algorithms facts for the 3, 4 and 8x tables (Continue to practise other Develop a reliable written method 12 15 for division Write and calculate Solve problems involving missing mathematical statements for Repeated subtraction - chunking numbers division using what is known Solve problems including those Use division facts to derive related division facts e.g. using that involve scaling Ensure children see/understand the link $6 \div 3 = 2$ to work out $60 \div 3 = 20$ Recognise, find and name 1/2 and 1/4 between grouping on a number line of an object, shape or quantity and vertical recording for chunking Understand the link between unit Vocabulary: equal groups of, fractions and division divided by, lots of, divide, divisible by, factor, division, $95 \div 5 = 19$ Connect 1/10 to division by 10 halve, half, share equally, dividend, divisor, quotient Count in tenths 95 arrays (10×5) TO ÷ O $48 \div 4$ Year 4 HTO ÷ O 45 Continue to practise recalling division facts for multiplication (<u>5</u> x 5) - 25 tables up to 12 x 12 Become fluent in the formal 4 written method of short division 20 **Fact Box** Practise mental methods and with exact answers when dividing extend this to three-digit by a one-digit number numbers for example 200 x 3 = $2 \times 5 = 10$ $-20 (4 \times 5)$ Divide one- or two-digit numbers $600 \text{ into } 600 \div 3 = 200$ by 10 or 100, identifying value of $5 \times 5 = 25$ 0 Use place value, known and digits as tenths or hundredths derived facts to divide mentally, Solve two-step problems in $10 \times 5 = 50$ including dividing by 1 different contexts, choosing the Recognise and use factor pairs appropriate operation, working Progressing to short division- no remainders and commutativity in mental with increasingly harder numbers including correspondence questions e.g. three cakes shared equally between 10 children $560 \div 4$ Vocabulary: equal groups of, divided by, lots of, quotient, divide, divisible by, factor, division, halve, half, share See Appendix 1 – teaching short equally, dividend, divisor, bar models

Division - multiplication and division should be taught together- refer to structures of division

Possible concrete and visual **End of Year Expectations** Teacher Modelling/Children's Recording **Fluency** representation Divide numbers with Count backwards in steps Year 5 Children might use manipulatives alongside algorithms Cuisenaire to up to 4 digits by Os of powers of 10 for any represent scaling given number up to 1000000 Identify factors, including finding all factor $560 \div 4$ pairs of a number, and common factors of Count backwards with **Short division** two numbers positive and negative whole numbers through without remainder Practise and extend the formal written $564 \div 5$ zero 4 0 method of short division: numbers up to four-digits by a one-digit number and Practise mental interpret remainders appropriately for the calculation with context increasingly large numbers Interpret non-integer answers to division by expressing results in different ways Apply all multiplication according to the context, including with tables and related division remainders, as fractions, as decimals or by facts frequently, commit rounding as appropriate for the context them to memory and use remainder as a decimal them to confidently to Use multiplication and division as inverses make larger calculations Solve problems involving division including See Appendix 1 -Vocabulary: groups of, scaling down by simple fractions and arrays remainder as teaching short division divided by, lots of, left over, problems involving simple rates $4.8 \div 4$ a fraction quotient, divide, divisible by, with manipulatives factor, remainder, division, Divide whole numbers and those halve, half, share, dividend, involving decimals by 10, 100 & 1000 $560 \div 24$ divisor, quotient. Long division Divide numbers with Year 6 Practise division for larger up to 4 digits by TO numbers, using the formal 23 r8 2 3 8/24 (1/3) written methods of short Divide decimals up to twoand long division decimal places by O or TO 24 | 5 Continue to use all Divide numbers up to 4-digits by a 2-digit multiplication tables and whole number using formal written methods 4 division facts to maintain of long division, interpret remainders as fluency 0.1 whole numbers, fractions or by rounding, as Perform mental appropriate for the context calculations, including Divide numbers with up to 2 decimal places with mixed operations and by 1-digit and 2-digit whole numbers, initially larger numbers in practical contexts involving money and measures Vocabulary: groups of, Understand the relationship between unit 0.8 divided by, lots of, left over, fractions and division quotient, divide, divisible Recognise division calculations as the inverse by, factor, remainder, of multiplication remainder as a remainder as a fraction division, halve, half, share, 0.8 dividend, divisor, quotient Solve problems involving division whole number in its lowest form

bar models

Moving to written algorithms Short Division – no exchange



Moving to written algorithms Short Division – with exchange

